

Porovnání zadaných příkladů v Počítačových algebraických systémech (PAS):

Maple 9.51, Derive 6, Mathematica

Zjednodusování: - Příklad c. 1 -

-

> reset;

reset

> a:=(sqrt(x*y*abs(z)^2))/(sqrt(x)*abs(z));

$$a := \frac{\sqrt{xy}}{\sqrt{x}}$$

> simplify(a, assume=positive);

$$\sqrt{y}$$

> expand(a);

$$\frac{\sqrt{xy}}{\sqrt{x}}$$

> combine(a);

$$\frac{\sqrt{xy}}{\sqrt{x}}$$

Derive 6:

$$\sqrt{y}$$

Mathematica:

$$\frac{\sqrt{xy}}{\sqrt{x}}$$

pokud bude kladné x:

$$\sqrt{y}$$

Příklad c.: 2:

a) z komplexní

-

-

> z:='z';

z:= z

> b:=ln(exp(z));

$b := \ln(e^z)$

`> simplify(b, assume=complexcons);`

$\ln(e^z)$

Derive 6:

$\text{LN}(e^z)$

Mathematica 5.1:

$\text{Log}[e^z]$

b) z reálné

`>`

`> simplify(b, assume=real);`

z

Derive 6:

z

Mathematica 5.1:

z

c) $z = 10i$

`> z:=10*I;`

$z := 10 I$

`> evalf(z);`

$10. I$

`>`

`> evalf(b);`

$\ln(e^z)$

`> simplify(b);`

$10 I - 4 I \pi$

`> subs(z=10*I, b);`

$\ln(e^{(10 I)})$

`> simplify(b);`

$\ln(e^z)$

`>`

Derive 6:

$2 \cdot i \cdot (5 - 2 \cdot \text{Pi})$

Mathematica 5.1:

$$-2i(-5 + 2\pi)$$

Příklad c. 3:

```
> c:='c';
```

```
c:=c
```

```
> z:='z';
```

```
z:=z
```

```
> c:=sqrt(z)-(z^3)^(1/6);
```

```
c:=sqrt(z)-(z^3)^(1/6)
```

```
> R1 := simplify( z^(1/2)-(z^3)^(1/6), 'assume=nonnegative' );
```

```
R1:=0
```

a) z - komplexní

```
> assume(z, complexcons);
```

```
> simplify(c);
```

```
sqrt(z~)-(z~^3)^(1/6)
```

Derive:

#30: $\sqrt{z} - (z^3)^{1/6}$

3 1/6

Mathematica 5.1:

```
sqrt(z)-(z^3)^(1/6)
```

b) z - realne

```
> assume(z, real);
```

```
> simplify(c);
```

```
-sqrt(z~)(-1+signum(z~))
```

Derive:

Mathematica 5.1:

$\sqrt{z} - \sqrt{z} \bullet \text{SIGN}(z)$

```
sqrt(z)-(z^3)^(1/6)
```

c) z - kladné

```
> assume(z, positive);
```

```
> simplify(c);
```

0

```
Derive: 0
```

```
Mathematica 5.1: 0
```

```
d) z = 999983
```

```
> subs(z=999983, c);
```

c

```
> R2 := evalf[100]( 999983^(1/2)-999949000866995087^(1/6) );
```

R2:= 0.

```
Derive: 0
```

```
Mathematica 5.1: 0
```

Příklad c. 4 – řešení rovnic, nerovnic:

První rovnice (nerovnice):

```
> prvni := abs(x^2-5*x+4) > 1;
```

$$prvni := 1 < |x^2 - 5x + 4|$$

```
> solve(prvni, x);
```

$$\text{RealRange}\left(-\infty, \text{Open}\left(\frac{5}{2} - \frac{1}{2}\sqrt{13}\right)\right), \text{RealRange}\left(\text{Open}\left(\frac{5}{2} + \frac{1}{2}\sqrt{13}\right), \infty\right), \\ \text{RealRange}\left(\text{Open}\left(\frac{5}{2} - \frac{1}{2}\sqrt{5}\right), \text{Open}\left(\frac{5}{2} + \frac{1}{2}\sqrt{5}\right)\right)$$

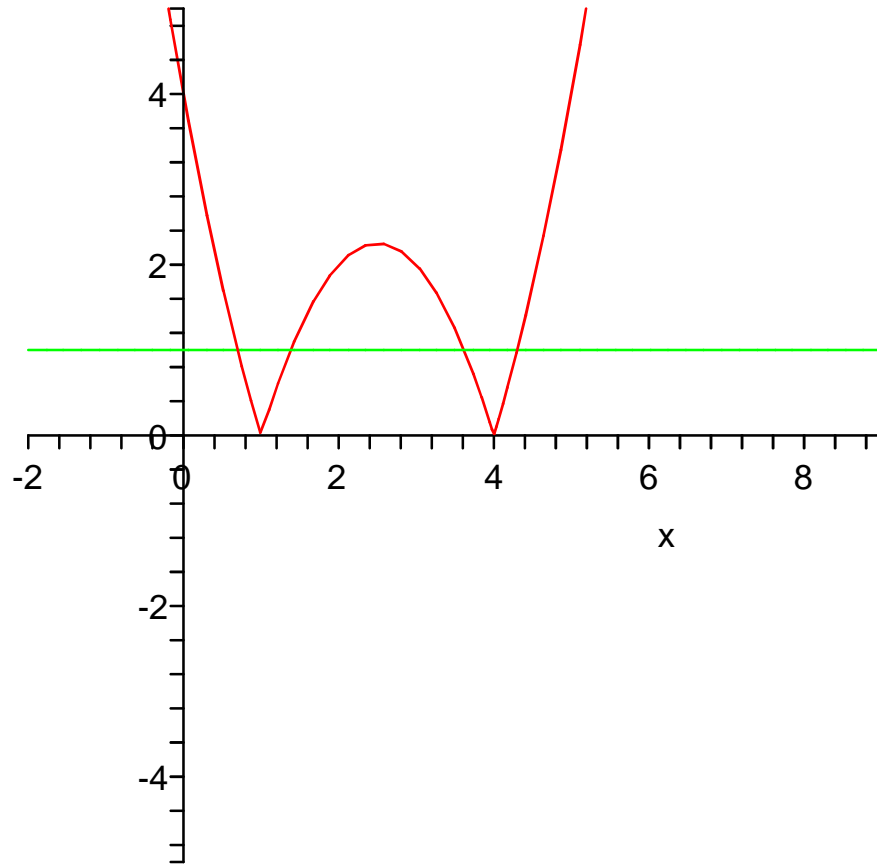
```
> evalf(solve(prvni, {x}));
```

{x < 0.697224362, {4.302775638 < x}, {x < 3.618033988 1.381966012 < x}

```
> R6 := `union`({x < 5/2-1/2*13^(1/2)}, {5/2+1/2*13^(1/2) < x},  
{5/2-1/2*5^(1/2) < x, x < 5/2+1/2*5^(1/2)});
```

$$R6 := \left\{ x < \frac{5}{2} - \frac{1}{2}\sqrt{13}, \frac{5}{2} + \frac{1}{2}\sqrt{13} < x, \frac{5}{2} - \frac{1}{2}\sqrt{5} < x, x < \frac{5}{2} + \frac{1}{2}\sqrt{5} \right\}$$

```
> plot([abs(x^2-5*x+4), 1], x=-2..9, -5..5);
```



Derive: $x < 0.6972243622 \vee 1.381966011 < x < 3.618033988 \vee x > 4.302775637$

Mathematica 5.1:

$$x < \frac{1}{2} (5 - \sqrt{13}) \vee \frac{1}{2} (5 - \sqrt{5}) < x < \frac{1}{2} (5 + \sqrt{5}) \vee x > \frac{1}{2} (5 + \sqrt{13})$$

Druha rovnice:



```
> x:='x';
```

```
x:=x
```

```
> druha:= sin(x) = tan(x);
```

```
druha := sin(x) = tan(x)
```

```
> R9 := solve( {sin(x) = tan(x)}, x);
```

```
R9:= {x = 0}
```

```
> _EnvAllSolutions := true;
```

`_EnvAllSolutions := true`

```
> solve(sin(x)=tan(x), x);
```

$\pi_Z1 \sim$

```
> about(indets(% , name));
```

```
{Pi, _Z1}:
```

is used in the following assumed objects

[Pi] assumed Pi

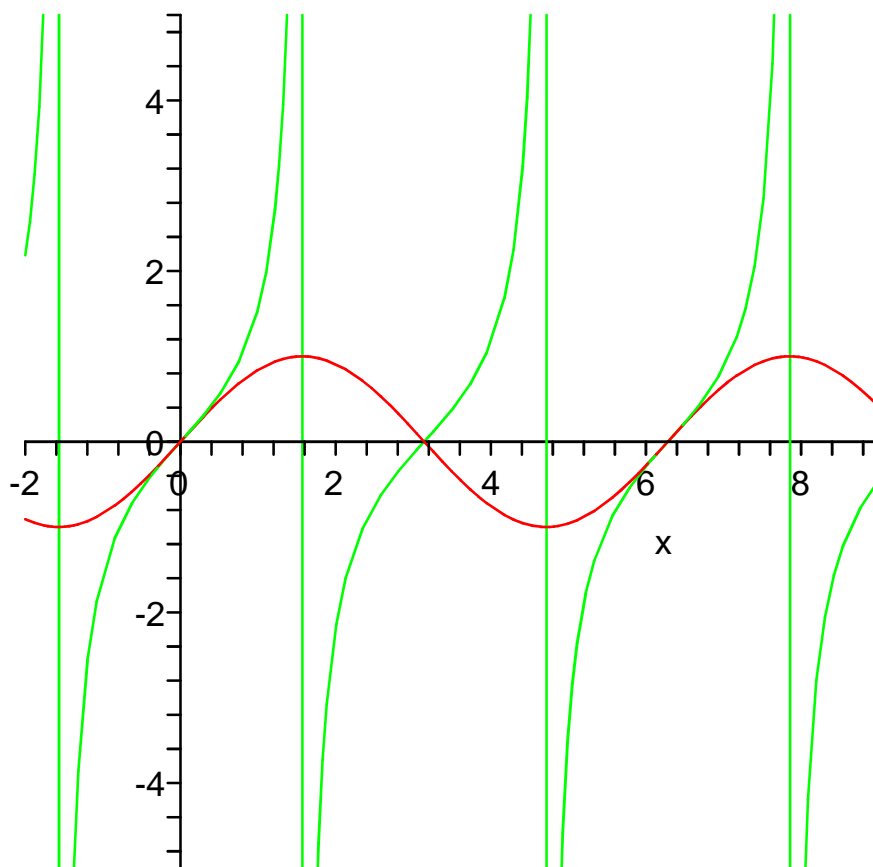
[_Z1] assumed integer

Derive: $x = -2\bullet\text{Pi} \vee x = 2\bullet\text{Pi} \vee x = -\text{Pi} \vee x = \text{Pi} \vee x = 0$

Mathematica 5.1:

```
C[1] ∈ Integers && (x == 2 π C[1] || x == π + 2 π C[1])
```

```
> plot([sin(x), tan(x)], x=-2..9,-5..5);
```



Treti rovnice:



```
> treti := (x^2-1)*(ln(x))*(sin(x))^3*(cos(x))^2 = 0;
      treti:= (x2 - 1) ln(x) sin(x)3 cos(x)2 = 0
```

```
> R12 := solve( {(x^2-1)*ln(x)*sin(x)^3*cos(x)^2 = 0} );
      R12:= {x = 1}, {x = -1}, { x =  $\frac{1}{2} \pi - \pi_{B1\sim} + 2 \pi_{Z2\sim}$  }, {x =  $\pi_{Z3\sim}$ }
```

Derive:

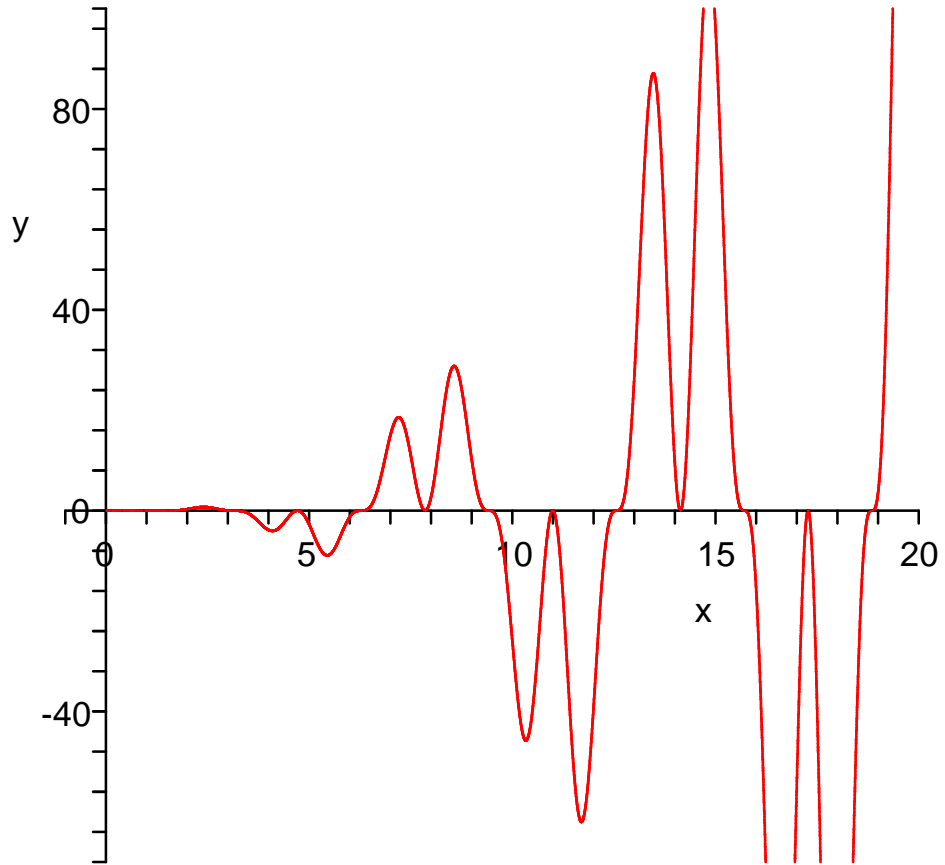
$$x = \frac{3 \cdot \pi}{2} \vee x = -\frac{\pi}{2} \vee x = \frac{\pi}{2} \vee x = -\pi \vee x = \pi \vee x = -1 \vee x =$$

$$\vee x = 0$$

Mathematica 5.1:

$$\left(C[1] \in \text{Integers} \ \&\& \ x \neq 0 \ \&\& \ \left(x = -\frac{\pi}{2} + 2\pi C[1] \ || \ x = \frac{\pi}{2} + 2\pi C[1] \right. \right. \\ \left. \left. x = 2\pi C[1] \ || \ x = \pi + 2\pi C[1] \right) \right) \ || \ x = -1 \ || \ x = 1$$

```
> plot((x^2-1)*(ln(x))*(sin(x))^3*(cos(x))^2, x=-1..20, y=-70..100,
      numpoints=10000, resolution=2000);
```



Ctvrta rovnice:

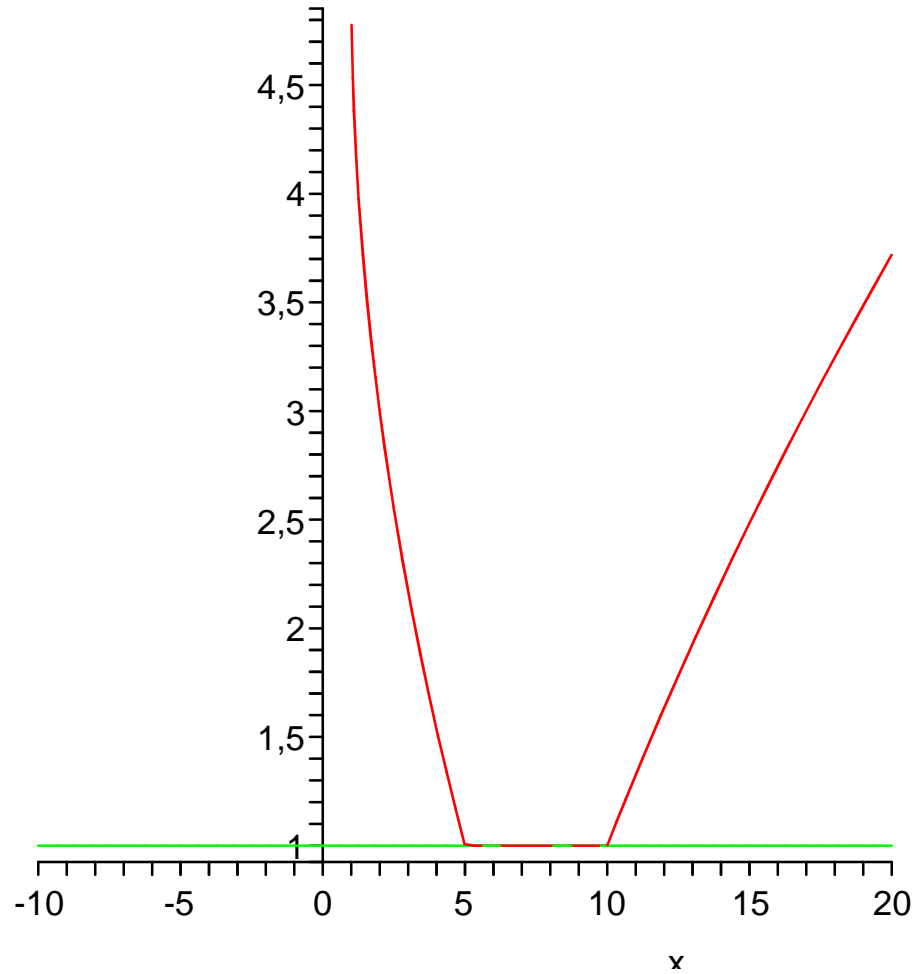
```
> sqrt(x+8-6*(sqrt(x-1)))+sqrt(x+3-4*sqrt(x-1))=1;
```

$$\sqrt{x+8-6\sqrt{x-1}} + \sqrt{x+3-4\sqrt{x-1}} = 1$$

```
> R1 := solve( {(x+8-6*(x-1)^(1/2))^(1/2)+(x+3-4*(x-1)^(1/2))^(1/2) = 1} );
```

$$R1 := \{x = x\}$$

```
> plot([(x+8-6*(x-1)^(1/2))^(1/2)+(x+3-4*(x-1)^(1/2))^(1/2), 1], x=-10..20);
```

```
> f := (x+8-6*(x-1)^(1/2))^(1/2)+(x+3-4*(x-1)^(1/2))^(1/2) = 1;
```

$$f := \sqrt{x+8-6\sqrt{x-1}} + \sqrt{x+3-4\sqrt{x-1}} = 1$$

```
> unassign(x);
```

```
> nerov := (x+8-6*(x-1)^(1/2))^(1/2)+(x+3-4*(x-1)^(1/2))^(1/2) <= 1;
```

$$\text{nerov} := \sqrt{x+8-6\sqrt{x-1}} + \sqrt{x+3-4\sqrt{x-1}} \leq 1$$

```
> solve(nerov, x);
```

RealRange(5, 10)

```
> solve(nerov, {x});
```

$\{5 \leq x, x \leq 10\}$

Derive: $5 \leq x \leq 10$

Mathematica 5.1:

$5 \leq x \leq 10$

Derivace a integrály

```
> x:='x';
```

```
x:= x
```

— Příklad c. 5:

```
> restart;
```

```
> with(Student[Precalculus]);
```

```
> with(Student[Calculus1]);
```

```
> f:=abs(x);
```

```
f:= |x|
```

```
> diff(f,x);
```

```
abs(1, x)
```

```
> Diff(f,x);
```

$$\frac{d}{dx} |x|$$

```
> int(f,x);
```

$$\begin{cases} -\frac{1}{2}x^2 & x \leq 0 \\ \frac{1}{2}x^2 & 0 < x \end{cases}$$

Derive:

x·SIGN(x)

Mathematica 5.1:

S tímto typem příkladu má Mathematica potíže, musel bych

ji to manuálně rozdelit...

— Příklad c. 6:

```
> 2*x*(x^2+1)^24;
```

```
2 x (x2 + 1)24
```

```
> R3 := int(2*x*(x^2+1)^24, x);
```

```
R3:= 81719 x18 + x2 + 43263 x16 + 19228 x14 + 178296 x22 + 178296 x28  
+ 208012 x24 + 92 x6 + 19228 x36 + 12 x4 + 208012 x26 + 43263 x34 + 506 x30  
+ 92 x44 + 12 x46 + 7084 x38 + 7084 x12 + 81719 x32 +  $\frac{653752}{5} x^{30}$ 
```

$$+ \frac{653752}{5} x^{20} + \frac{1}{25} x^{50} + \frac{10626}{5} x^{10} + x^{48} + \frac{10626}{5} x^{40} + 506 x^{42}$$

> **R3:=combine(R3, power);**

$$\begin{aligned} R3 := & 81719 x^{18} + x^2 + 43263 x^{16} + 19228 x^{14} + 178296 x^{22} + 178296 x^{28} \\ & + 208012 x^{24} + 92 x^6 + 19228 x^{36} + 12 x^4 + 208012 x^{26} + 43263 x^{34} + 506 x^{40} \\ & + 92 x^{44} + 12 x^{46} + 7084 x^{38} + 7084 x^{12} + 81719 x^{32} + \frac{653752}{5} x^{30} \\ & + \frac{653752}{5} x^{20} + \frac{1}{25} x^{50} + \frac{10626}{5} x^{10} + x^{48} + \frac{10626}{5} x^{40} + 506 x^{42} \end{aligned}$$

Kontrola z toho, co jsem vypocital v ruce:

> **(x^2+1)^25/25;**

$$\frac{1}{25} (x^2 + 1)^{25}$$

> **R0 := simplify(1/25*(x^2+1)^25);**

$$R0 := \frac{1}{25} (x^2 + 1)^{25}$$

> **R1 := expand(1/25*(x^2+1)^25);**

$$\begin{aligned} R1 := & 81719 x^{18} + x^2 + 43263 x^{16} + 19228 x^{14} + 178296 x^{22} + 178296 x^{28} \\ & + 208012 x^{24} + 92 x^6 + 19228 x^{36} + 12 x^4 + 208012 x^{26} + 43263 x^{34} + 506 x^{40} \\ & + 92 x^{44} + 12 x^{46} + 7084 x^{38} + 7084 x^{12} + 81719 x^{32} + \frac{653752}{5} x^{30} \\ & + \frac{653752}{5} x^{20} + \frac{1}{25} + \frac{1}{25} x^{50} + \frac{10626}{5} x^{10} + x^{48} + \frac{10626}{5} x^{40} + 506 x^{42} \end{aligned}$$

> **R1-R3;**

$$\frac{1}{25}$$

>

Derive:

$$\frac{(x^2 + 1)^{25}}{25} + c$$

Mathematica 5.1:

$$2 \left(\frac{x^2}{2} + 6x^4 + 46x^6 + 253x^8 + \frac{5313x^{10}}{5} + 3542x^{12} + \right. \\
9614x^{14} + \frac{43263x^{16}}{2} + \frac{81719x^{18}}{2} + \frac{326876x^{20}}{5} + \\
89148x^{22} + 104006x^{24} + 104006x^{26} + 89148x^{28} + \\
\frac{326876x^{30}}{5} + \frac{81719x^{32}}{2} + \frac{43263x^{34}}{2} + 9614x^{36} + \\
\left. 3542x^{38} + \frac{5313x^{40}}{5} + 253x^{42} + 46x^{44} + 6x^{46} + \frac{x^{48}}{2} + \frac{x^{50}}{50} \right)$$

Příklad c. 7:

```
> Int7:=Int(1/x^(1/3),x=-1..1);
```

$$Int7 := \int_{-1}^1 \frac{1}{x^{(1/3)}} dx$$

```
> value(Int7);
simplify(%);
```

$$-\frac{3}{2}(-1)^{(2/3)} + \frac{3}{2} \\
\frac{9}{4} - \frac{3}{4}i\sqrt{3}$$

```
> Int7a:=Int(surd(1/x, 3),x=-1..1):%=value(%);
```

$$\int_{-1}^1 \operatorname{surd}\left(\frac{1}{x}, 3\right) dx = 0$$

Derive: 0

Mathematica 5.1:

$$-\frac{3}{2} \left(-1 + (-1)^{2/3} \right)$$

Příklad c.8:

`> with(inttrans);`

`[adddtable, fourier, fouriercos, fouriersin, hankel, hilbert, invfourier, invhilbert, invlaplac, invmellin, laplace, mellin, savetable]`

`obraz k z=cos(omega*t+phi)`

`> o:=cos(omega*t+phi);`

$$o := \cos(\omega t + \phi)$$

`> laplace(o, t, p);`

$$\frac{\cos(\phi) p - \sin(\phi) \omega}{p^2 + \omega^2}$$

Derive:

$$\frac{(s \cdot \cos(\phi) - \omega \cdot \sin(\phi))}{s^2 + \omega^2}$$

Mathematica 5.1:

$$\frac{p \cos[\phi] - \sqrt{\omega^2} \text{Sign}[\omega] \sin[\phi]}{p^2 + \omega^2}$$

`vzor k (ap+b)/(p^2+p+1)`

`> v:=(a*p+t)/(p^2+p+1);`

$$v := \frac{a p + t}{p^2 + p + 1}$$

`> invlaplace(v, p, t);`

$$\frac{1}{3} e^{\left(-\frac{1}{2} t\right)} \left(3 a \cos\left(\frac{1}{2} \sqrt{3} t\right) + \sqrt{3} \sin\left(\frac{1}{2} \sqrt{3} t\right) (-a + 2 t) \right)$$

Derive: Zde se prapodivnými cestami dostáváme k úplnému nesmyslu..., prostě to neumí efektivně a celé najednou udělat ani s pomocným balíčkem:

--- při zadání celého výrazu najdenou nedokázal PC předložit výsledek ani za 2 hodiny nepřetržitého počítání, přičemž se pak PC restartoval. Prováděno na: Celeron(R) 3,06 GHz

Mathematica 5.1:

$$\frac{1}{3} e^{-t/2} \left(3 a \cos\left[\frac{\sqrt{3} t}{2}\right] - \sqrt{3} (a - 2 b) \sin\left[\frac{\sqrt{3} t}{2}\right] \right)$$

Příklad c.9:

```

> M:={seq(5*k+1, k=1..30)};
M:= {6, 11, 16, 21, 26, 31, 36, 41, 46, 51, 56, 61, 66, 71, 76, 81, 86, 91, 96, 101, 106, 111
116, 121, 126, 131, 136, 141, 146, 151}

> S:=2:
for i to 100
do
if isprime(i)
then S:=S,i;
fi;
od;
S;
P:={S};
2, 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
P:= {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89,
97}

> M intersect P;
{11, 31, 41, 61, 71}

```

Derive:P = {1, 3, ..., 100}

#106: P

#107: {1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 35,
37, 39, 41, 43, 45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, 67,
69, 71, 73, 75, 77, 79, 81, 83, 85, 87, 89, 91, 93, 95, 97, 99}

#108: M = 5•k + 1

#109: k = {1, ..., 30}

#110: M = {{5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80,
85, 90, 95, 100, 105, 110, 115, 120, 125, 130, 135, 140, 145, 150}
+ 1}

#111: P ∩ M

#112: {5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85,
90, 95, 100, 105, 110, 115, 120, 125, 130, 135, 140, 145, 150} + 1
∩ {1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33,
35, 37, 39, 41, 43, 45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65,

67, 69, 71, 73, 75, 77, 79, 81, 83, 85, 87, 89, 91, 93, 95, 97, 99}

---- také takové zvláštní :-)

Mathematica 5.1:

```
M = Table[5 * k + 1, {k, 30}]
```

```
{6, 11, 16, 21, 26, 31, 36, 41, 46, 51, 56, 61, 66, 71, 76, 81, 86  
91, 96, 101, 106, 111, 116, 121, 126, 131, 136, 141, 146, 151}
```

```
{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37,  
41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97}
```

```
{11, 31, 41, 61, 71}
```

Příklad c.10:

-

```
> with(Logic);  
[&and, &if, &implies, &nand, &nor, &not, &or, &xor, BooleanSimplify, Canonicalize,  
Contradiction, Dual, Environment, Equal, Equivalent, Export, Implies, Import,  
Normalize, Random, Satisfy, Tautology, TruthTable]
```

```
> a &or &not a;  
BooleanSimplify(%);
```

```
a &or &not(a)  
true
```

Derive: True

Mathematica: True

```
> a &or b &or (a &and b);  
BooleanSimplify(%);
```

```
(a &or b) &or (a &and b)  
a &or b
```

Derive: $a \vee b$

Mathematica:

```
a || b
```

```
> not Equivalent(a,c) or (b and c and d) or (a and c and (b\d));  
not Equivalent(a, c) or b and c and d or a and c and bd
```

Derive: $(d \cap f \vee \neg c \vee (d \wedge f) \vee \neg e) \wedge (c \vee e)$ //pouzita
pismena posunuta od a,b

Mathematica 5.1:

```
a # c || b c c c d || a c c c ! (b c d)
```

>

Závěr:

-

Pokud mám porovnat systémy, které jsme měli možnost v tomto předmětu ozkoušet, rozdělil bych to ze dvou hledisek. Pokud potřebuji jenom něco malého intuitivně a rychle naklikat a spočítat, považuji Derive za poměrně dobrou volbu, ovšem s nevýhodou, že to není software k dispozici volně ani pro studenty.

Maple ale co jsem měl možnost vidět v nové verzi 10.0 šlape v této výhodě Derivu silně na paty, jelikož pro typicky "klickačské" výpočty má k dispozici kalkulátor, který je docel "user friendly". Pro složitější výpočty je pro mě Maple jasná volba, například jak je zapracováno na rovnicích s absolutní hodnotou je velmi slušné.

Při porovnávání Mathematiky jsem možná poněkud zaujatý, ale přijde mi to jako strašně nepohodlný program oproti třeba Maplu. Prostě jsem se s ní nedokázal sžít, spíše naopak... :-)

Matematické programy jsou ale vesměs užitečné a vyplatí se spíše než počítání v ruce, i když je někdy třeba obezřetnosti.